NRT/KS/19/2183

Bachelor of Science (B.Sc.) Semester—VI Examination OPERATIONS RESEARCH Optional Paper—1 (Statistics)

Time : Three Hours]

[Maximum Marks : 50

10

10

N.B. :— All questions are compulsory and carry equal marks.

- 1. (A) What is critical path ? Explain different types of float associated with activities in network. What will be float for critical activity ?
 - (B) Explain looping and dangling in the Network analysis with the help of network diagram. How these can be avoided ? 5+5

OR

(E) Discuss PERT analysis.

2. (A) Define cost-slope of an activity. How is cost slope used in crashing the project ? Which activity should be preferentially crashed ? Which activity when crashed will not reduce project duration ?

OR

- (E) If for certain feasible solutions to the primal and dual their respective objective functions attain same value, then prove that the feasible solutions are optimum solutions.
- (F) For a primal-dual pair, if there exists an optimum solution to either, then there exists optimum solution to other.
 5+5
- 3. (A) Prove that a transportation problem has a triangular basis.
 - (B) Describe the Vogel's approximation method used for finding initial basic feasible solution to a transportation problem.
 5+5

OR

- (E) Prove that necessary and sufficient condition for transportation problem to attain a feasible solution is that it should be balanced.
- (F) Discuss North-West Corner Rule for determining the initial basic feasible solution to a transportation problem. When will the solution be degenerate ? 5+5
- 4. (A) Discuss Hungarian method for obtaining an optimal solution of an assignment problem. 10

OR

- (E) Define competitive game. Give two real life situations where game-theory can be applied. Define a two person zero sum game.
- (F) Define the terms :
 - (i) Player
 - (ii) Strategy
 - (iii) Optimum strategy
 - (iv) Mixed-strategy
 - (v) Pure strategy.

- 5. Solve any **TEN** of the following questions :
 - (A) Distinguish between float and slack.
 - (B) State two uses of dummy activity.
 - (C) Which events will always have zero slack?
 - (D) Stating whether the following statements are true or false, rewrite the correct statements :
 - (i) Dual of a dual LPP is again a dual problem.
 - (ii) If a primal has an unbounded objective function then dual has no feasible solution.
 - (E) If a LPP consists of 3 constraints with 5 variables, which one will be easy to solve, the given LPP or its dual? Give reason for the answer.
 - (F) Which activity or activities should be crashed, as and when, there are multiple critical paths, to reduce the project duration ?
 - (G) Define a loop in a transportation table.
 - (H) What could be the number of positive allocations in a transportation problem for the solution to be basic feasible; given that the problem has m-sources and n-destinations.
 - (I) In a transportation problem there are 7-sources and 8-destinations. State the number of allocations in a non-degenerate basic feasible solution for this problem.
 - (J) What is 'minimax' strategy ?
 - (K) In a two person (A and B) zero sum game, is it necessary to construct payoff matrix for both players ? Why ?
 - (L) When will an assignment problem have an alternate optimal solution ? $1 \times 10=10$